

# On the Effect of Local Grain-Boundary Chemistry on the Macroscopic Mechanical Properties of a High-Purity $\text{Y}_2\text{O}_3\text{-Al}_2\text{O}_3\text{-Containing Silicon Nitride Ceramic: Role of Oxygen}$

A. Ziegler and J. M. McNaney

Materials Science and Technology Division, Lawrence Livermore National Laboratory, Livermore, California 94551

M. J. Hoffmann

Institut für Keramik im Maschinenbau, Universität Karlsruhe, D-76131 Karlsruhe, Germany

R. O. Ritchie<sup>†</sup>

Materials Sciences Division, Lawrence Berkeley National Laboratory, and Department of Materials Science and Engineering, University of California, Berkeley, California 94720

The effects of grain-boundary chemistry on the mechanical properties of high-purity silicon nitride ceramics have been investigated, specifically involving the role of oxygen, present along the grain boundaries, in influencing the fracture behavior. To avoid complications from inadvertently introduced impurities, studies were performed on a high-purity  $\text{Si}_3\text{N}_4$  processed using two-step gas-pressure-HIP sintering. Varying the grain-boundary oxygen content, which was achieved by control of oxidizing heat treatments and sintering additives, was found to result in a transition in fracture mechanism, from transgranular to intergranular fracture, with an associated increase in fracture toughness. This phenomenon is correlated to an oxygen-induced change in grain-boundary chemistry and possibly to a concomitant structural transformation along the interface. The incorporation of oxygen appears to affect fracture by “weakening” the interface, thus facilitating debonding and crack advance along the boundaries, and hence to toughening by grain bridging. It is concluded that if the oxygen content in the thin grain-boundary films exceeds a lower limit, which is  $\sim 0.87$  equiv% oxygen content, then the interfacial structure and bonding characteristics favor intergranular debonding during crack propagation; otherwise, transgranular fracture ensues.

## I. Introduction

THE properties of silicon nitride ceramics are strongly influenced by microstructure and the chemical composition of the grain-boundary phase. Indeed, during processing, the grain boundary is the key microstructural feature that dictates the mechanical properties. It has long been recognized that the room-temperature strength and toughness of monolithic  $\text{Si}_3\text{N}_4$  ceramic materials depend strongly upon the microstructure and crack path. Generally, fine-grained materials exhibit the highest strength, while high toughness is promoted by large-grained microstructures and an intergranular fracture path. Whereas strength is commonly associated with flaw size, which is invariably related to grain size, toughness is generally attributed to dissipative mechanisms acting behind the crack tip, including

grain bridging and frictional pull-out.<sup>1–17</sup> Consequently, a microstructure of fine, elongated grains that fails intergranularly generally provides both high toughness and good strength. The precise reasons why a ceramic fails intergranularly, as opposed to transgranularly, however, are still uncertain, although the predominant view is that by “weakening” the interface, debonding and crack advance along the boundaries are facilitated. Accordingly, interface strength and crack path must be controlled by the chemical composition, atomic structure, and bonding along the grain-boundary phase.

In this work, we examine two highly pure  $\text{Si}_3\text{N}_4$  ceramics, containing  $\text{Y}_2\text{O}_3$  and  $\text{Al}_2\text{O}_3$  as additives, and specifically investigate the change in fracture mechanism and crack path, which is critical to defining the mechanical properties, in terms of the effect of (i) post-sintering heat treatments and (ii) slight variations in grain-boundary composition. Our approach is to focus on the role of *local* grain-boundary chemistry and its relation to crack propagation and *macroscopic* mechanical properties.

## II. Background

Grain boundaries in most silicon nitrides have a typical width of 1–5 nm. This equilibrium size is considered to be a function of chemical composition<sup>18–26</sup> rather than the amount of additive; processing parameters, such as sintering temperature, time, and pressure, appear to have little effect. The additives tend to segregate along boundaries and accumulate at the triple junctions.<sup>27–29</sup> Oxygen also accumulates at the boundaries, and is assumed to have a marked effect (possibly more significant than that of other sintering additives) on the mechanical properties.

Post-sintering heat treatments have invariably been found to improve the strength, creep, and toughness properties of  $\text{Si}_3\text{N}_4$  ceramics<sup>30–38</sup>, sound explanations as to why this happens have been generally inconclusive, in part due to the complexity of the oxidation/devitrification processes that occur during such heat treatments. A partially crystallized boundary phase usually exists at multiple-grain junctions, while the remainder of the liquid sintering aid solidifies as a thin amorphous film between the crystalline phases.<sup>27–30</sup> Thermodynamic considerations of the specific local chemistry and interfacial atomic structure govern the existence of these amorphous films.<sup>39</sup> The devitrification of the grain boundaries and the effects that it has on the mechanical properties have suggested two different explanations for the improvements in strength and toughness.<sup>40–49</sup> The first argues that the structure and bonding characteristics of the thin grain-boundary films are critical in governing the strength and tough-

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<sup>†</sup>Author to whom correspondence should be addressed. e-mail: RORitchie@LBL.gov

ness of the bulk ceramic.<sup>40–45</sup> As post-sintering heat treatments can alter the local atomic structure and bonding along the thin grain boundaries, this can promote debonding there, leading to intergranular fracture and toughening from grain bridging. An alternative explanation involves the mismatch of thermal expansion coefficients between the crystallized, or partially crystallized, triple points, the thin amorphous grain-boundary films, and the matrix grains.<sup>46–49</sup> As the thermal expansion coefficient of the amorphous grain-boundary film is high compared with that of the adjacent grains, the contraction of the crystalline intergranular material is larger than that of the corresponding amorphous phase, resulting in tensile residual stresses, capable of initiating cracking in, and adjacent to, the boundary, particularly in the vicinity of the partially crystalline triple junctions. It is conceivable that both mechanisms operate *in concert*, with the tensile residual stresses promoting crack initiation and the local bonding promoting crack growth along the boundaries.

During oxidizing heat treatments, oxygen diffuses into the microstructure while sintering aid cations diffuse outward to the surface.<sup>50–53</sup> It has been suggested that oxygen replaces nitrogen at the grain boundary and its interfaces with neighboring matrix grains.<sup>54–57</sup> This would be in agreement with calculated binding energies of Si-tetrahedral clusters with various N:O ratios, showing that the Si–O bond will provide the most reduction in energy and therefore will be more favorable than the Si–N bond.<sup>54</sup> Similarly, with Al–O and Al–N tetrahedral clusters, Al–O will exhibit the stronger bond. The binding energy of  $\text{SiN}_x\text{O}_y$  and  $\text{AlN}_x\text{O}_y$  clusters increases systematically when O substitutes for N. Hence, of the tetrahedral structures, the four structures  $\text{SiO}_4$ ,  $\text{SiNO}_3$ ,  $\text{SiN}_2\text{O}_2$ , and  $\text{AlO}_4$  are theoretically the most stable.<sup>54</sup> These results are in good agreement with nuclear magnetic resonance studies of Si–Al–Y oxynitride glasses, showing that the glass films are made up of  $\text{SiO}_4$ ,  $\text{SiNO}_3$ ,  $\text{SiN}_2\text{O}_2$ , and  $\text{AlO}_4$  tetrahedra.<sup>55</sup> Consequently, each oxygen atom added to  $\text{Si}_3\text{N}_4$ , containing among its sintering additives  $\text{Al}_2\text{O}_3$ , would introduce an additional Si–O or Al–O cross bond; as replacements for Si–N, or Al–N-type cross-bonds, they would act to *strengthen* interfacial cohesion. In contrast, studies on the debonding behavior of  $\beta\text{-Si}_3\text{N}_4$  whiskers in Si–Al–Y oxynitride glass have shown that a decrease in the N:O ratio *weakens* interfacial cohesion.<sup>45,46</sup>

Such theoretical calculations assume a simplified model of pure Si–O–N glass. The reality is quite different though, as actual grain-boundary phases are (i) composed of more than just Si, O, and N atoms and (ii) they are confined to a few nanometers in width. Moreover, their atomic structure has to connect to differently oriented  $\text{Si}_3\text{N}_4$  matrix grains on both sides. To date, no investigation has examined the correlation between oxygen content and grain-boundary weakening in a real, dense  $\text{Si}_3\text{N}_4$  ceramic with typically very thin grain boundaries. This is a major objective of the present study, and is achieved by using heat treatment to vary the oxygen content along the grain boundaries.

### III. Experimental Procedures

#### (1) Materials and Heat Treatment

Conventional densification processing of silicon nitride ceramics generally has used glass encapsulation, resulting in the introduction of impurity elements originating from the glass encapsulation of the green body. To minimize this problem,  $\text{Si}_3\text{N}_4$  ceramics in the present study were uniquely fabricated without glass encapsulation, resulting in a highly pure material with very controlled amounts of sintering additives. Specifically, fabrication was achieved via a two-step gas pressure sintering and a subsequent hot-isostatic-pressing densification technique.<sup>58</sup> Such high-purity, controlled processing, with impurity-free densification, was utilized to discern the specific role of small quantities of sintering additions. Two different  $\text{Si}_3\text{N}_4$  compositions were examined, containing  $\text{Y}_2\text{O}_3$  and  $\text{Al}_2\text{O}_3$  as sintering additives. The two compositions are designated as (2/0/1) and

(2/0/0) by the nominal amount and type of sintering additive ( $\text{Y}_2\text{O}_3/\text{SiO}_2/\text{Al}_2\text{O}_3$ ), as described in Table I. Although not intentionally added,  $\text{SiO}_2$  is an inherent component of the ceramic body as the  $\text{Si}_3\text{N}_4$  powder particles are covered by a fine  $\text{SiO}_2$  layer. The resulting microstructures of both compositions consisted of exclusively  $\beta\text{-Si}_3\text{N}_4$  in both acicular-shaped and equiaxed grains (Fig. 1).

In addition to the as-sintered material, a set of samples of the same batch was subjected to a post-sintering heat treatment of varying duration (25, 50, 100, and 200 h) at  $1400^\circ\text{C}$  in air. Based on studies of the microstructure and oxide formation, this heat treatment was selected so that both the transition to and the final chemical/microstructural equilibrium state could be examined. The average grain size, determined according to ASTM E112-96, and aspect ratios before and after heat treatment are listed in Table II.

#### (2) Mechanical Testing

Hardness and fracture toughness properties were measured using indentation techniques, the toughness being evaluated by inducing crack formation under a standard Vickers indenter using 5, 7, 10, 12, and 15 kg loads. Twenty-five indents per sample (five indents per load), resulting in a total of 1050 crack lengths, were measured under an optical microscope, with the hardness,  $H$ , and indentation fracture toughness,  $K_{\text{IC}}$ , calculated using the relationships<sup>5</sup>:

$$H = \frac{P}{2 \times \left(\frac{a}{2}\right)^2} \quad (1)$$

$$K_{\text{IC}} = 0.016 \times \left(\frac{E}{H}\right)^{1/2} \times \frac{P}{\left(\frac{c}{2}\right)^{3/2}} \quad (2)$$

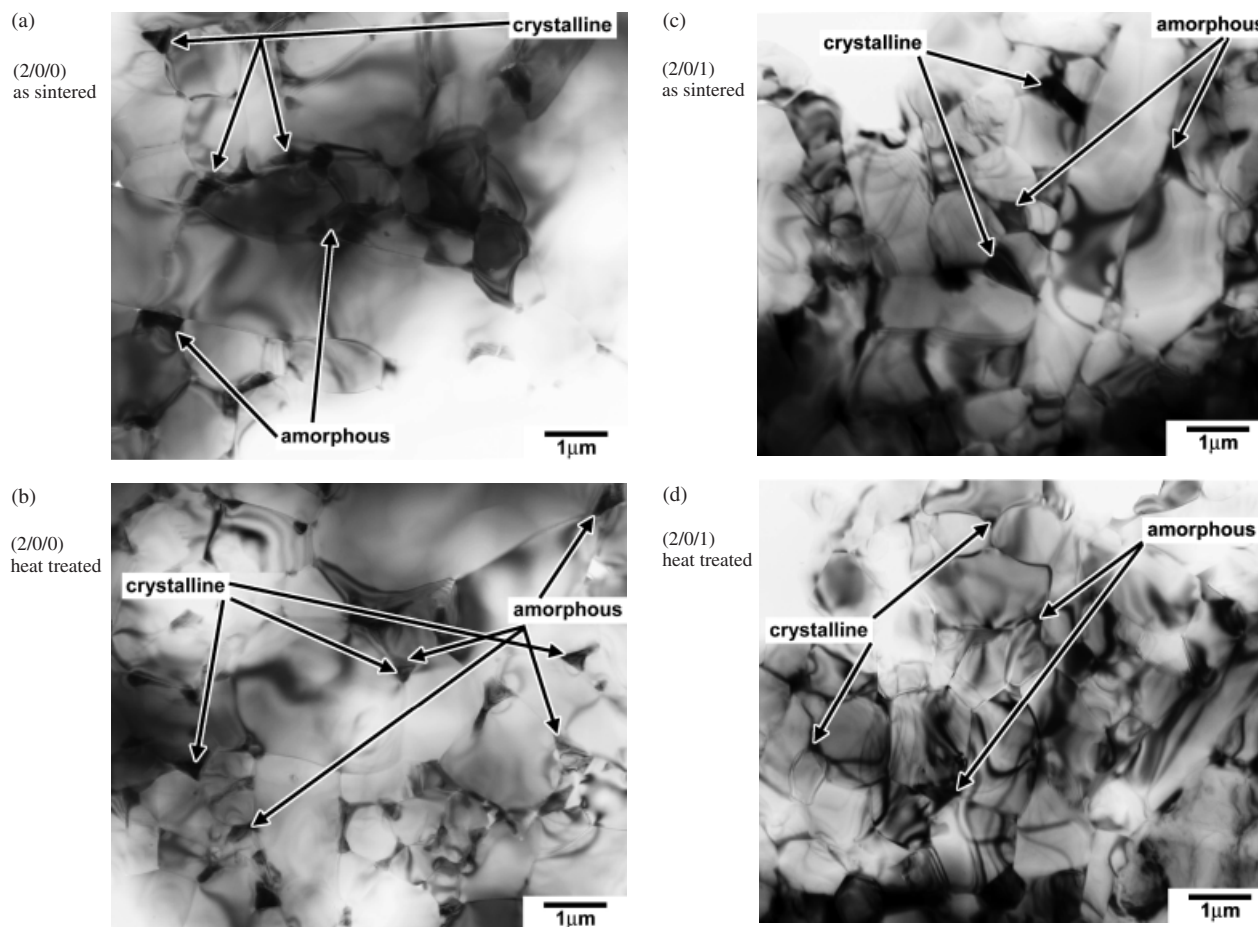
where  $P$  is the applied load,  $E$  is the Young's modulus (taken to be 300 GPa),  $a$  is the diagonal of the Vickers indent, and  $c$  is the total length of the crack extending from the corners of the indent. By determining the toughness over a range of indentation loads, i.e., over a range of crack sizes, an estimate of the resistance-curve ( $R$ -curve) behavior was obtained.

#### (3) Characterization

Energy-dispersive X-ray emission spectroscopy (EDX) was carried out on thin transmission electron microscopy (TEM) samples in a Philips CM200/FEG TEM (Hillsborough, OR) to discern the distribution of chemical elements along and across the boundaries. With the EDX detector (Oxford Microanalysis 6767, Oxford, UK), spatially resolved compositional analysis ( $Z < 5$ ) could be performed with an energy resolution of 136 eV for  $\text{MnK}\alpha$  radiation. The EDX probe diameter could be focused to a 1.2 nm small spot to detect the signal emanating from a 1–5 nm thin grain-boundary film. EDX spectra were collected by (i) line scans across the thin grain boundaries and (ii) spectra covering an area of  $20 \text{ nm} \times 20 \text{ nm}$  from approximately the center of the triple junctions. On each specimen, five spectra on the grain boundaries and five spectra on the triple points were collected. For the spectra measured on thin grain boundaries, it was necessary to align the grain boundary as edge-on as possible, usually by orienting the grain to one side of it along a low index zone axis, i.e., mostly [0001]. Effects like beam broadening and

**Table I. Silicon Nitride Material Compositions Investigated in this Study**

	Nominal composition (wt%)				Mol (mol%)			
	$\text{Si}_3\text{N}_4$	$\text{Y}_2\text{O}_3$	$\text{SiO}_2$	$\text{Al}_2\text{O}_3$	$\text{Si}_3\text{N}_4$	$\text{Y}_2\text{O}_3$	$\text{SiO}_2$	$\text{Al}_2\text{O}_3$
(2/0/1)	97.0	2.0	0	1.0	97.4	1.2	0	1.4
(2/0/0)	98.0	2.0	0	0	98.7	1.3	0	0



**Fig. 1.** TEM images of the microstructure of both material compositions in their as-sintered and 200 h heat-treated states, respectively, (a, b) (2/0/0) and (c, d) (2/0/1). The arrows indicate crystalline and amorphous triple points.

sampling depth are negligible when collecting the EDX signal in a TEM, because the TEM specimen thickness is usually much less than the EDX excitation depth and thus, beam broadening is insignificant. The individual EDX spectra were background normalized.

Scanning electron microscopy (SEM) of the fracture surfaces was performed using a JEOL 6300 scanning electron microscope (Tokyo, Japan). SEM was also used to measure the oxide layer thickness after heat-treatment cycles to assess the oxidation behavior. In order to measure this layer thickness, the samples were broken, instead of cut, along the fracture surfaces; contrast differences between the bulk material and the oxide layer helped in measuring the layer thickness.

#### IV. Results and Discussion

##### (1) Toughness and Fractography

Except for grain-boundary chemistry, the microstructures of the initial as-sintered (2/0/1) and (2/0/0) compositions differ only in grain size (Fig. 1); whereas the grain aspect ratio is the same, the Al-containing (2/0/1) material exhibits a factor of two smaller

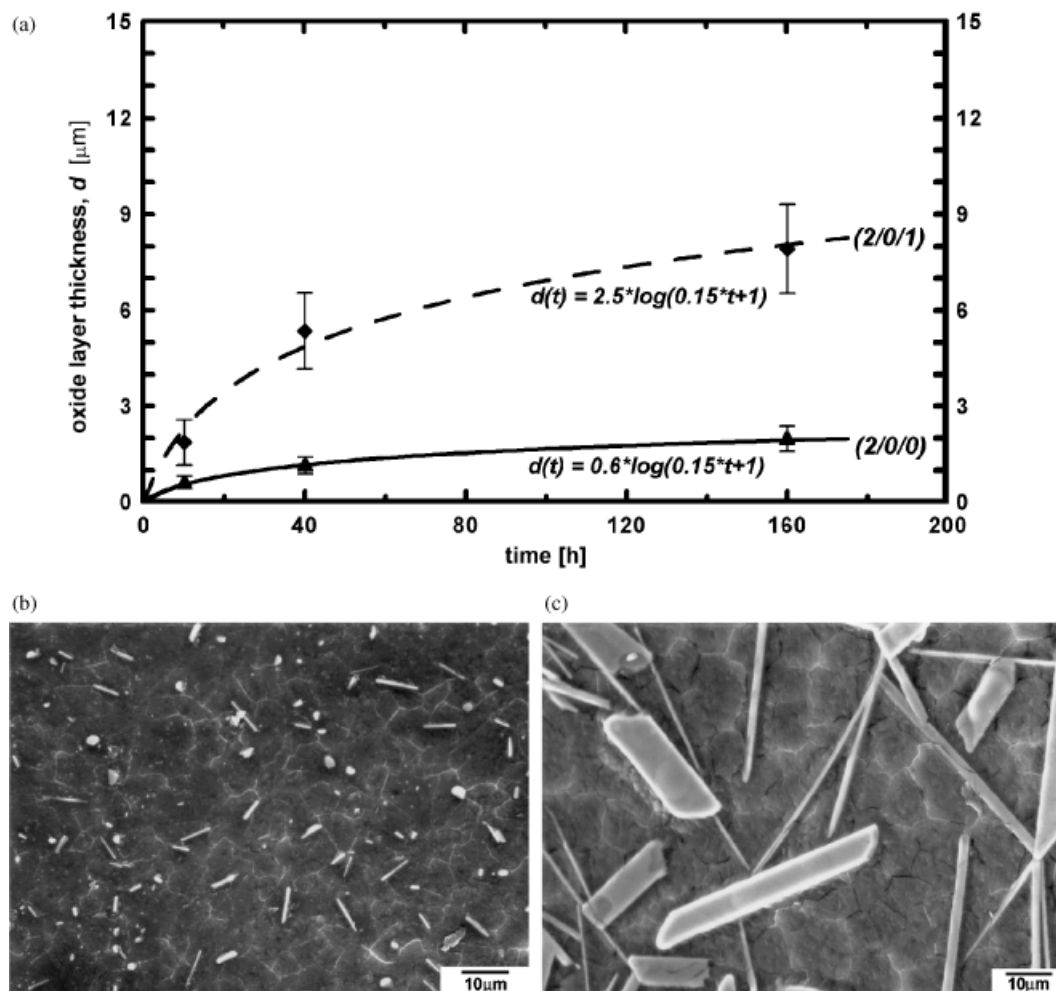
grain size than the Al-free (2/0/0) material (Table II). Following the oxidizing heat treatments, the morphology of these microstructures appeared unchanged; there was no additional grain growth, no microstructural coarsening, and no change in aspect ratio (Table II). With respect to the morphology of the triple points, any differences after heat treatment were not considered to be significant; only a few triple points crystallized and many amorphous triple points were still seen, even after 200 h at 1400°C in both (2/0/1) and (2/0/0) compositions (Fig. 1). These images show how the amount of grain-boundary phase is distributed among triple points and thin two-grain grain boundaries; the triple points have a larger capacity than the thin films to encompass this secondary phase.

The effect of oxidation during the 1400°C heat treatments is presented in Fig. 2. The primary purpose was to assess the overall oxidation behavior of the two  $\text{Si}_3\text{N}_4$  variants and to confirm that their oxidation behavior is comparable to other  $\text{Si}_3\text{N}_4$  ceramics. The surface oxidation rates at 1400°C, measured as the growth of oxide layer thickness over time, indicate a logarithmic oxidation law, which is consistent with diffusion-controlled oxidation through the growing oxide scale.<sup>59–64</sup> The scale itself consists primarily of amorphous  $\text{SiO}_2$ , embedded with differently sized, elongated  $\text{Y}_2\text{Si}_2\text{O}_7$  crystals, the majority of which are pure crystals although some also contain Al. In Fig. 2, it can also be seen that the growth of the surface oxide layer depends on the grain-boundary chemistry, especially with respect to the presence (or absence) of  $\text{Al}_2\text{O}_3$ . Whereas the  $\text{Al}_2\text{O}_3$ -free (2/0/0) material had only thin oxide scales ( $< 2 \mu\text{m}$ ), the  $\text{Al}_2\text{O}_3$ -containing (2/0/1) samples exhibited a pronounced growth in surface oxide, with a layer thickness up to 8  $\mu\text{m}$ . The diffusion paths in  $\text{Si}_3\text{N}_4$  are primarily the grain boundaries, since at high temperatures, the thin amorphous intergranular films tend to become viscous and facilitate diffusion. The formation of the

**Table II.** Average Grain Sizes and Aspect Ratios

Composition	Average grain size ( $\mu\text{m}$ )		Aspect ratio	
	a.s.	h.t.	a.s.	h.t.
(2/0/1)	2	2	8	8.1
(2/0/0)	4.1	3.9	8.3	8.2

a.s., as-sintered; h.t., heat treated.



**Fig. 2.** Oxidation behavior of the material compositions considered in this investigation, showing (a) the growth and thickness of the surface oxide layer and (b) and (c) the formation of the elongated  $\text{Y}_2\text{Si}_2\text{O}_7$  surface crystals after (b) 10 h and (c) 160 h on the surface of the (2/0/0) material.

observed surface crystals clearly indicates that Y and Al, and O for that matter, are diffusing along these grain boundaries, which presumably allows for those elements to move to energetically more favorable atomic locations associated with a different chemical bonding state.

The results of the hardness and indentation fracture toughness measurements on both the as-sintered and heat-treated materials are presented in Fig. 3. The hardness (Figs. 3(a),(b)) shows only a marginal decline with increasing indentation load (and hence crack length). Usually at low loads, indentation cracking occurs during unloading; at high loads, however, cracking can occur prematurely during loading, leading to larger indents and hence lower apparent hardness. The results show that the overall effect of grain-boundary chemistry and heat treatment on hardness is minimal for the different  $\text{Si}_3\text{N}_4$  materials examined.

In contrast, the toughness is significantly affected by grain-boundary chemistry (Figs. 3(c),(d)). In the as-sintered state, the (2/0/1) material clearly shows stable initial crack growth, in that the fracture toughness increases with crack length in the form of rising  $R$ -curve behavior. Conversely, the (2/0/0) material shows no evidence of such behavior, with unstable fracture occurring immediately at crack initiation. However, with heat treatment, these marked differences gradually disappear, as the (2/0/0) material undergoes a marked change in fracture behavior that completely changes the shape of its  $R$ -curve and results in an  $\sim 180\%$  increase in toughness compared with its as-sintered value. Indeed, after 200 h at  $1400^\circ\text{C}$ , the (2/0/0) material exhibits rising  $R$ -curve behavior and a fracture toughness comparable to that of the (2/0/1) material. In contrast, the evolution of the (2/0/1) material with heat treatment is less dramatic, with only a

maximum  $\sim 15\%$  increase in toughness and no change in shape of the  $R$ -curve.

Fractography of the indented and subsequently fractured samples is presented in Figs. 4 and 5. They reveal that the as-sintered (2/0/0) material exhibits a brittle transgranular fracture surface, with no features of grain pull-out and interlocking grains that are typical of many toughened ceramic materials. After heat treatment though, the (2/0/0) composition shows a distinct change in fracture mode, from largely transgranular to largely intergranular. In contrast, fracture in the (2/0/1) material remains predominantly intergranular before and after heat treatment. The intergranular crack paths are consistent with toughening in the crack wake via crack bridging from interlocking grains that act to shield the crack tip from the applied far-field load.<sup>1-3,6-16</sup> Since the bridging is a function of crack size, this is also consistent with the observed  $R$ -curve behavior in Figs. 3(c) and (d), where the materials display increasing toughness with increasing crack length.

The relatively high toughness of the heat-treated (2/0/0) material, particularly at large crack lengths, can be associated with its larger grain size, as compared with the (2/0/1) material; provided fracture occurs intergranularly, coarse-grained microstructures (with high aspect-ratio grains) are more effective in promoting crack bridging, which acts to inhibit crack extension.<sup>3,6-10</sup> In the as-sintered state, however, such grain-size arguments do not apply as the (2/0/0) material fails transgranularly and hence cannot develop any crack-tip shielding from crack bridging; under these circumstances, the toughness remains low with no rising  $R$ -curve behavior. Thus, irrespective of microstructural parameters such as grain size and aspect ratio, crack-bridging mechanisms in monolithic ceramics can only be

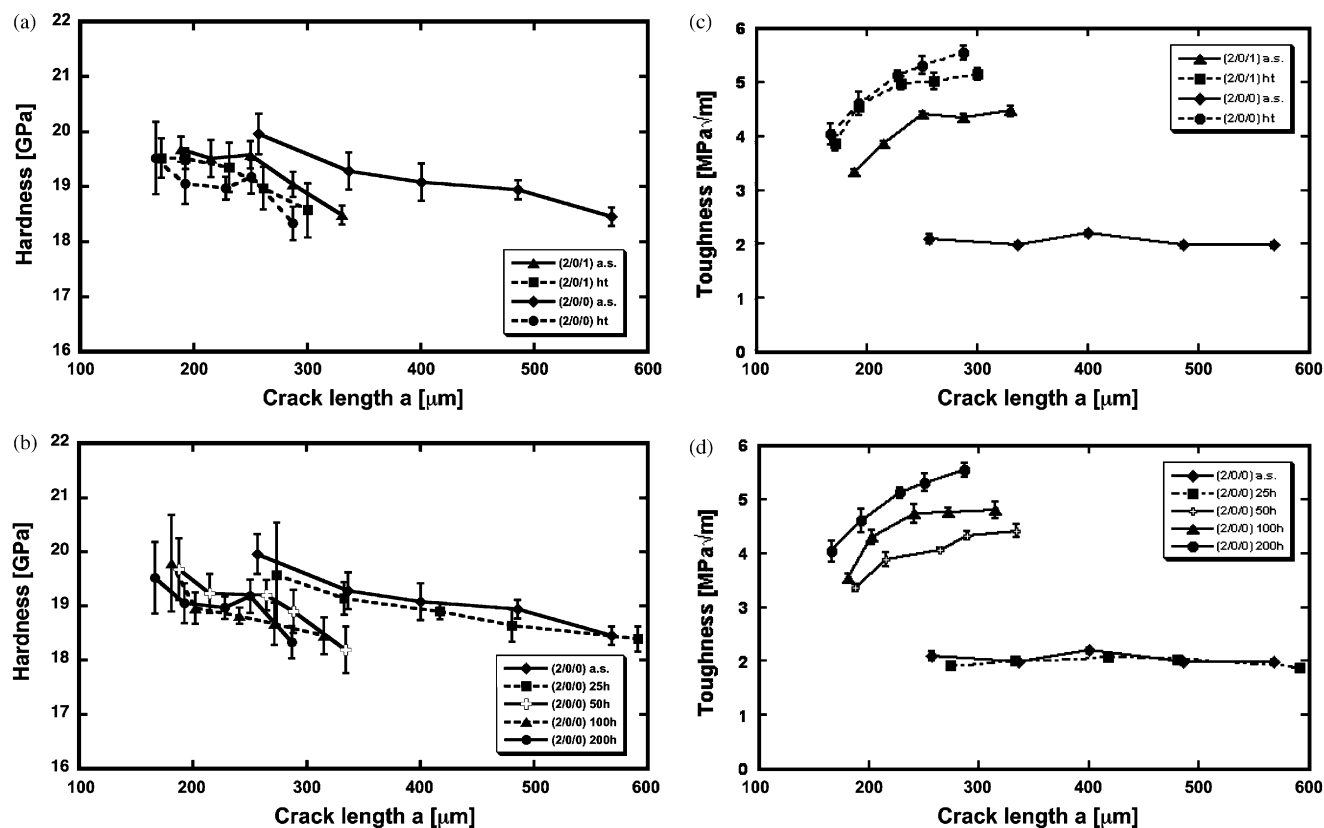


Fig. 3. (a, b) Hardness and (c, d) indentation fracture toughness values for both material compositions in their as-sintered and the heat-treated states.

active if the crack path is intergranular. The nature of the crack path is therefore a central issue, which depends strongly on how the grain-boundary chemistry determines the debonding characteristics.

Whereas the strength, toughness, and fractographic data for the (2/0/0) and (2/0/1) materials are in general agreement with existing notions<sup>3</sup> concerning the toughening of silicon nitrides, it remains to be understood exactly how grain-boundary chemis-

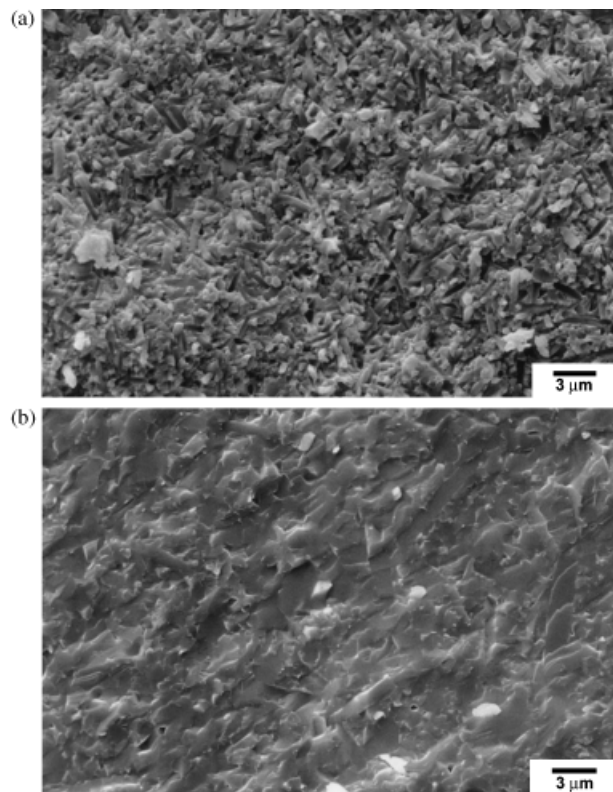


Fig. 4. Fracture surfaces of the as-sintered material compositions (a) (2/0/1) and (b) (2/0/0).

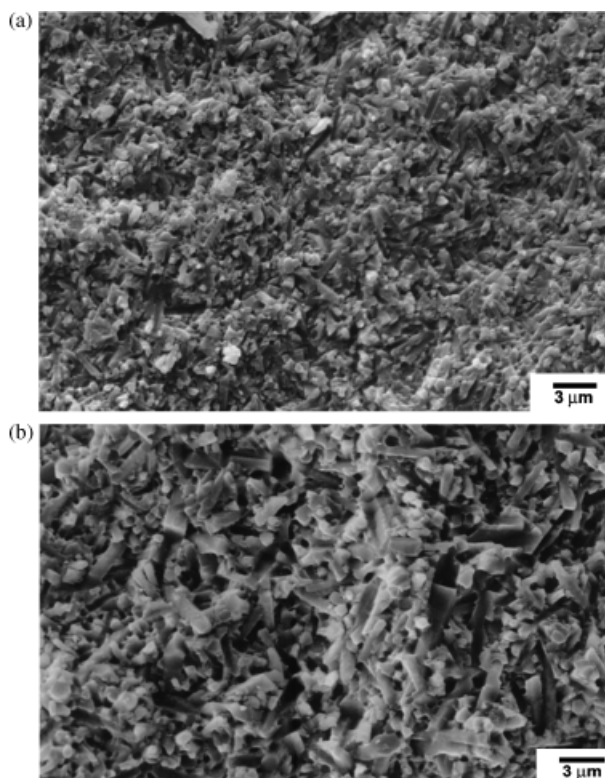


Fig. 5. Fracture surfaces of the heat-treated material compositions (a) (2/0/1) and (b) (2/0/0).



try can affect the choice of crack path. As noted above, in the present work, the use of very high-purity ceramics permits a more rigorous assessment of the chemical and structural factors governing this choice. Of particular interest are how the additives and heat treatment affect the grain-boundary chemistry, bonding, and structure, especially where there were no associated changes in grain size and shape. Two effects are worthy of consideration using detailed grain-boundary characterization:

(1) First, as the grain size and shape remain unchanged, it is clear that the marked increase in toughness and associated rising *R*-curve behavior of the (2/0/0) material after heat treatment follows from the fracture-path transition to intergranular fracture caused by a change in the local atomic structure and bonding characteristics along the boundary that promotes interfacial debonding. We presume here that the 1400°C heat treatment causes a rearrangement and relocation of specific atoms (sintering additives and oxidation products) along grain boundaries.

(2) Second, comparison of the as-sintered (2/0/1) and (2/0/0) materials is interesting as both contain the same amount of yttrium and yet differ by 1 wt%  $\text{Al}_2\text{O}_3$ , which is sufficient to cause a difference in fracture mode. With the addition of  $\text{Al}_2\text{O}_3$ , it is important to note that oxygen, as well as aluminum, may be inherently incorporated into the grain boundary.

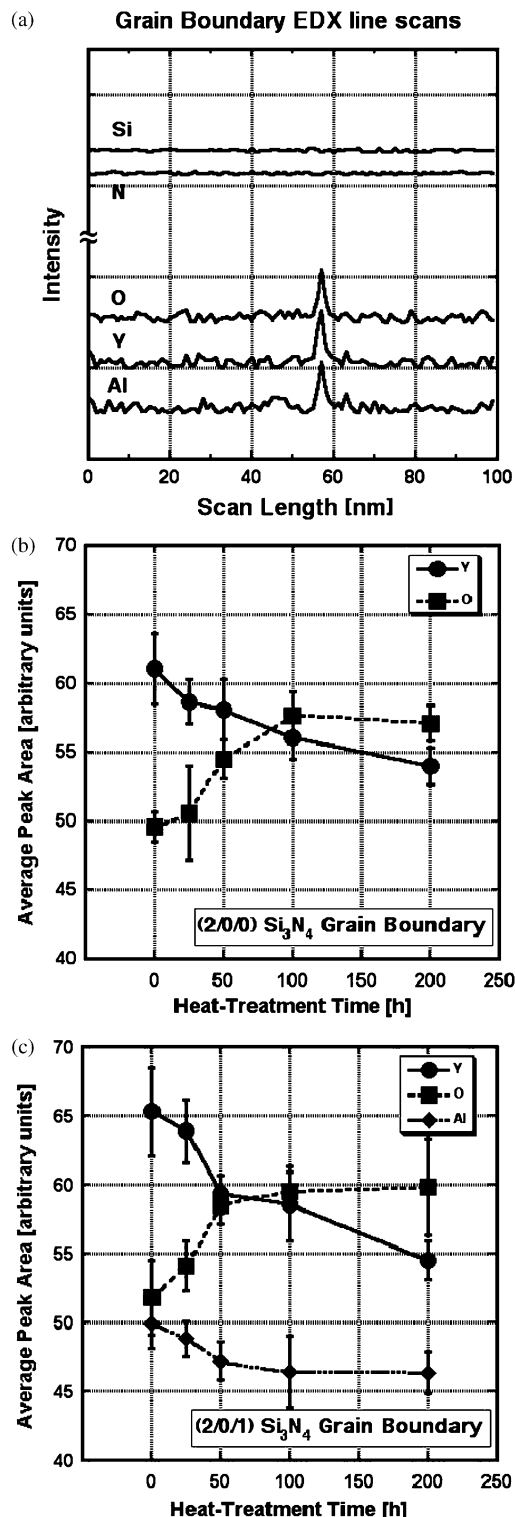
## (2) Grain-Boundary Analysis

Our hypothesis is that the observed change in fracture mechanism is associated with structural transformations in the grain-boundary phase that incorporate O, N, and the sintering-additive cations, or with the relocation of these ions. With the heat-treated materials, it can be assumed that O is the major element that diffuses inward while Y, Al, and N diffuse outward. Here, changes in the chemical balance and atom rearrangement are expected to only occur locally as the diffusion distances along the boundaries for these elements at 1400°C are only a few hundred micrometers. Consequently, since the possible variation in bonding is limited, we can assume that relocation of elements is more important than the inward or outward diffusion from the entire sample.

Our focus is on the short-range relocation of oxygen, yttrium, and aluminum, using EDX to analyze the elemental composition of the thin grain boundaries as they evolve during the heat treatment. In principle, the grain boundary is assumed to experience a critical structural transformation that markedly changes the bonding characteristics, allowing for either debonding or reinforcement of existing chemical bonds across the interface, which in turn determines the crack path—intergranular or transgranular.

The results of the EDX line scans across the thin grain boundaries are presented in Fig. 6. A single line scan immediately reveals the presence of yttrium segregated along the grain boundaries. Y, Al, and O could be measured as they are not encountered in the matrix and segregate entirely to the boundaries. In contrast, quantitative detection of Si and N levels across the grain boundaries could not be achieved as they are encountered in both the matrix and boundaries, and the strong Si and N signals from the matrix grains marred any slight changes in the thin grain boundaries (Fig. 6(a)).

Using the line scans performed on each specimen, the evolution of the grain-boundary chemical composition (Y, Al, and O) was monitored and is depicted in Figs. 6(b) and (c). To obtain this trend line, the spectra were background normalized and the area under each Y, Al, and O peak (not their peak height) was respectively measured for each heat-treatment stage. Each point on the trend line represents the average of five spectra per specimen. It is apparent from these results that in the Al-free material (2/0/0), yttrium tends to diffuse away from the thin grain boundaries as the heat treatment progresses, while the amount of oxygen increases between the grains; however, a considerable amount of yttrium remains along the thin boundaries. In the Al-containing material (2/0/1), similar observations can be made in that the amount of oxygen increases along the thin grain bound-



**Fig. 6.** (a) Example of an EDS line scan spectra revealing the detection of Y, O, and Al along the thin grain boundaries in a (2/0/1) specimen. Note that the intensity axis is not to scale. (b) and (c) show how the grain-boundary chemistry changes during heat treatment.

aries, while the corresponding amounts of Y and Al decrease; however, the rate of decrease in Al is slower than with Y.

The corresponding EDX trend lines obtained for the amorphous and crystalline triple points are shown in Figs. 7(a–d). The crystallized triple points examined in the as-sintered material were clearly formed during sintering. Only a few additional triple points crystallized during heat treatment (Fig. 1), leaving most in their amorphous state and allowing EDX analysis of both triple-point morphologies throughout the entire heat-treat-

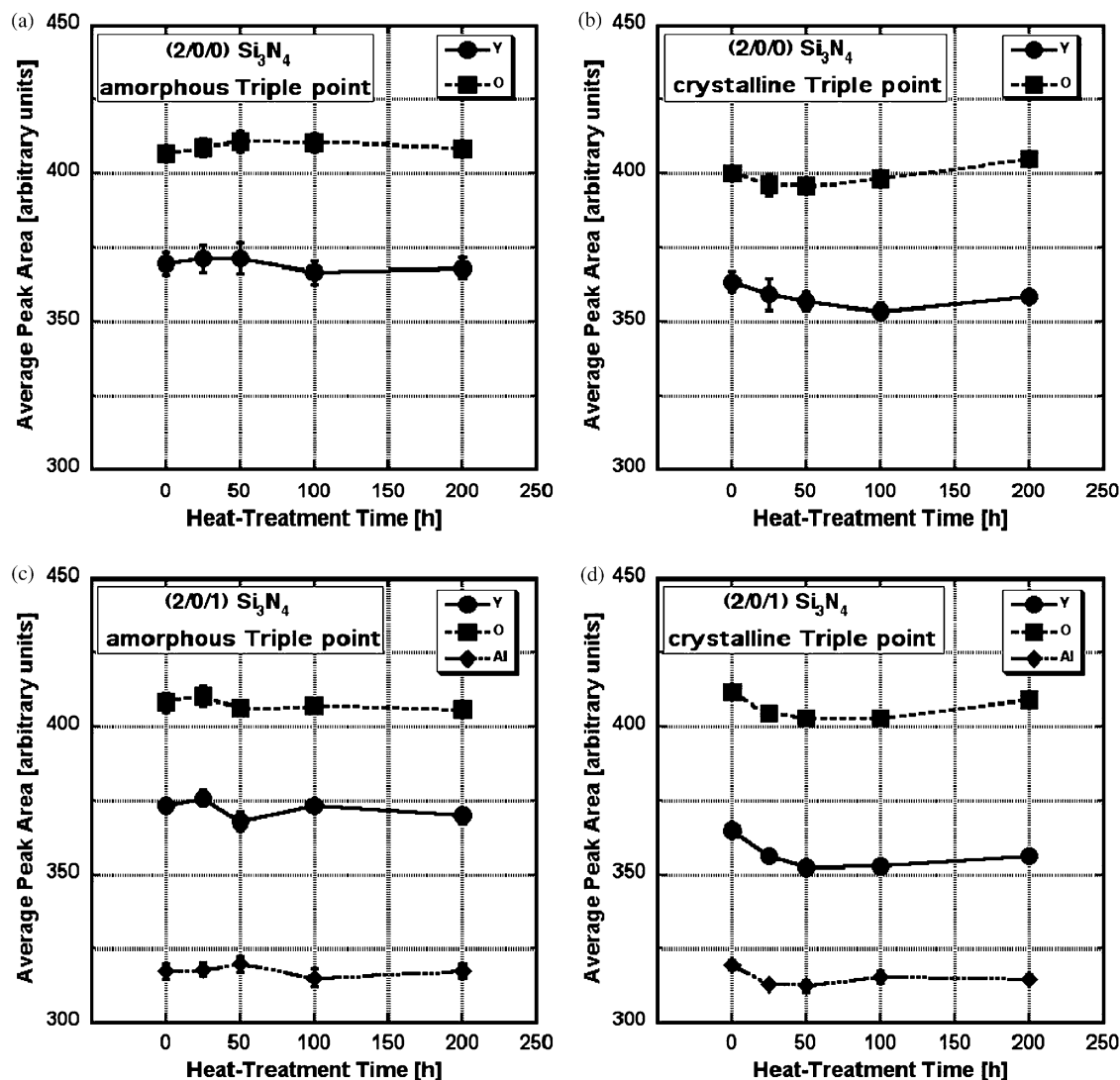


Fig. 7. EDS areal spectra of the triple points showing how the triple-point chemistry changes during heat treatment in the (a,b) (2/0/0) and (c,d) (2/0/1) material.

ment cycle. As seen in Fig. 7, both types of triple points show only marginal changes in their chemical composition during heat treatment. This is because they are regions that are much larger than the thin grain boundaries and therefore contain more grain-boundary phase (segregated chemical elements); as their EDX signal intensity is much stronger than the one emanating from the boundaries, small changes in the triple-point EDX signal intensity are more difficult to discern. The notion that the triple points and the thin grain boundaries are interconnected and thus their respective transformations and chemical balances influence each other can therefore only be examined by analyzing the changes in chemistry in the thin grain boundaries. This result, together with our observations of limited crystallization of the triple points, implies: (i) relative to the thin grain boundaries, the triple points can be regarded as reservoirs of grain-boundary phase and as a sink/source for O, N, Y, and Al cations, and (ii) for the present microstructures, the effects of triple-point crystallization on the mechanical properties are relatively unimportant.

The changes in the chemical balance and atom rearrangement that determine the fracture mode appear to occur at a very local level in the thin amorphous grain boundaries. How explicitly this modification and structural transformation occurs is the focus of continuing investigation. Similarly, it is important to know how the presence/absence of Al and Y cations affects the mechanical properties. It is known, however, that by increasing the amount of oxide-based sintering additives in this same

material, i.e., 3, 5, and 7 wt% Y<sub>2</sub>O<sub>3</sub>, fracture occurs intergranularly.<sup>65</sup> However, it is thought that the incorporation of oxygen into the grain-boundary structure is the primary factor to consider for a structural transformation that markedly changes the bonding and fracture characteristics. Since the observed change in fracture mode occurred as a consequence of the heat treatment, it can be concluded that oxygen is the governing element that affects fracture behavior in the (2/0/0) Si<sub>3</sub>N<sub>4</sub> material.

Such results are consistent with theoretical studies of the structure and bonding at grain boundaries in Si<sub>3</sub>N<sub>4</sub> ceramics.<sup>66–72</sup> Some of these calculations realistically focus on the incorporation of O into the grain-boundary phase, in keeping with observations that most, if not all, of these thin grain boundaries are found to contain oxygen. It is likely that the Si–N bonds are replaced by Si–O bonds and oxygen takes up the atom positions of nitrogen along the interface. The consequences of this substitution are clear. Experimental results collected in the present work, and in previous studies,<sup>45,46</sup> demonstrate that incorporation of more oxygen into the grain-boundary structure appears to facilitate intergranular debonding. The immediate question here, though, is whether there is a limit in grain-boundary oxygen content that determines whether the ceramic fractures transgranularly or intergranularly.

Table III lists estimated values for the overall oxygen and nitrogen content (in equiv%) and their ratios in both as-sintered (2/0/0) and (2/0/1) materials, obtained from the initial stoic-

**Table III. Ratios of Elements in the Si<sub>3</sub>N<sub>4</sub> Ceramics Studied**

	O/(Si+N+Y+O+(Al)) (eq%)	N/(Si+N+Y+O+(Al)) (eq%)
(2/0/0)	2.406	55.03
(2/0/1)	3.002	54.45

**Table IV. Statistical Microstructural Parameters**

	Relative area TP/GB	GB EDX signal (areal cps)	Increase in GB EDX signal (%)	GB oxygen content (eq%)
(2/0/0)				
a.s.	3.08	49.6	—	0.79
25 h	2.93	50.6	2.02	0.81
50 h	3.03	54.5	9.88	0.87
100 h	3.16	57.7	16.33	0.92
200 h	3.01	57.1	15.12	0.91
	3.04 ± 0.08			
(2/0/1)				
a.s.	2.86	51.8	—	1.04
25 h	2.84	54.1	4.44	1.09
50 h	2.91	58.5	12.93	1.17
100 h	2.97	59.5	14.86	1.19
200 h	2.90	59.8	15.44	1.20
	2.89 ± 0.05			

TP, triple point; GB, grain boundary; EDX, energy-dispersive X-ray emission spectroscopy; a.s., as-sintered.

hiometry when mixing the ceramic powders. These numbers cannot be taken as representative values for the oxygen content along the thin grain boundaries because the grain-boundary phase is also present at the triple points. Also, the oxygen content in the heat-treated samples cannot be quantitatively assessed because it is not known how much oxygen is actually absorbed by the grain boundaries during such heat treatment.

However, a qualitative analysis of the distribution of grain-boundary phase and consequently oxygen among triple points and thin grain boundaries can be performed. A critical assumption is that O is located only in, and is homogeneously distributed along, the grain-boundary phase, i.e., there is no clustering or preferential accumulation, for example, at triple points. To determine the relative volume of triple point versus thin grain boundary, the areas covered by the triple points and by the boundaries were estimated from low-magnification images of the microstructure.<sup>‡</sup> Three TEM images of each of the four microstructures studied were taken; results are listed in Table IV. It can be seen that the volume ratio of triple points to thin grain boundaries is approximately three. Thus, the overall oxygen content listed in Table III needs to be divided accordingly, leaving, for example, 0.79 equiv% of oxygen along thin grain boundaries in the as-sintered (2/0/0) material. Combining this relative content with the corresponding increase in EDX signals measured on the thin grain boundaries can yield estimates of how much oxygen is located in the thin films. These are listed in Table IV where it can be seen that after 50 h at 1400°C, the EDX signal for the (2/0/0) material has increased by 9.88% and the oxygen content along the thin films has increased to 0.87 equiv%. Although this is just a small increase, it is apparent that it is sufficient to locally change the bonding characteristics to such a degree that it causes a fracture mode transition and thereby affects the macroscopic fracture behavior.

The results in Table IV can also be used to estimate the limiting local oxygen content (or otherwise a limit for the nitrogen or a limiting N:O ratio) along the thin grain boundaries that influences the interfacial bond strength and thus affects the fracture-mode change from transgranular to intergranular, which in

turn affects the mechanical properties. In the (2/0/0) material, this limit is reached after 50 h at 1400°C when the material first displays rising *R*-curve behavior and intergranular fracture, i.e., at 0.87 equiv% oxygen. The (2/0/1) composition does not experience this change in fracture mode because its thin grain-boundary oxygen content is already above this critical limit in the as-sintered condition.

## V. Conclusions

In an attempt to identify relationships between local grain-boundary composition and macroscopic mechanical behavior, the present study has examined the effects of grain-boundary chemistry on the mechanical properties of two highly pure silicon nitride ceramics, containing, respectively, 2 wt% Y<sub>2</sub>O<sub>3</sub> and 2 wt% Y<sub>2</sub>O<sub>3</sub>/1 wt% Al<sub>2</sub>O<sub>3</sub>, where the grain-boundary oxygen content could be varied by the amount of sintering additives and by allowing oxygen diffusion from triple points into the grain boundaries during a post-sintering heat treatment. These Si<sub>3</sub>N<sub>4</sub> systems were selected because differences in macroscopic fracture behavior are primarily controlled by the grain-boundary oxygen content, rather than microstructural variations such as grain size and shape and crystallization of the triple points; moreover, the presence of intergranular, as opposed to transgranular, fracture is invariably a prerequisite for good fracture properties.

The local oxygen content along the thin grain boundaries was increased by diffusion from triple points during a post-sintering heat treatment at 1400°C. In the Al-free material, this resulted in a change in fracture mode from transgranular to intergranular with a concomitant improvement in mechanical properties; with no change in strength, the material displayed rising *R*-curve behavior with a dramatic increase in fracture toughness by ~180% (after 200 h at 1400°C). [In Si<sub>3</sub>N<sub>4</sub> ceramics, intergranular fracture is known to promote interlocking grains in the crack wake, which can enhance the (*R*-curve) toughness through a mechanism of crack bridging].

Such a marked change in mechanical properties was found to be associated with the incorporation of oxygen into the grain boundaries, where its role was to suitably "weaken" the interface, thereby facilitating debonding and intergranular crack advance. EDX analysis of the thin grain boundaries and the triple points revealed qualitative changes in grain-boundary chemistry, specifically the increase in oxygen content and decrease in yttrium and aluminum content during the 1400°C heat treatment. The assumption that there is a grain-boundary oxygen-content limit determining the change in fracture mode could be confirmed. It is concluded that if the incorporation of oxygen into the grain-boundary phase exceeds this (lower) limit, then the interfacial structure and bonding characteristics change in favor of intergranular debonding during crack propagation; otherwise, transgranular fracture occurs. By comparing the changes in fracture mode with the changes in grain-boundary oxygen content, this limit was estimated to be ~0.87 equiv% oxygen.

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